

# First-passage-based Last-passage Algorithm for Charge Density on a Conducting Surface

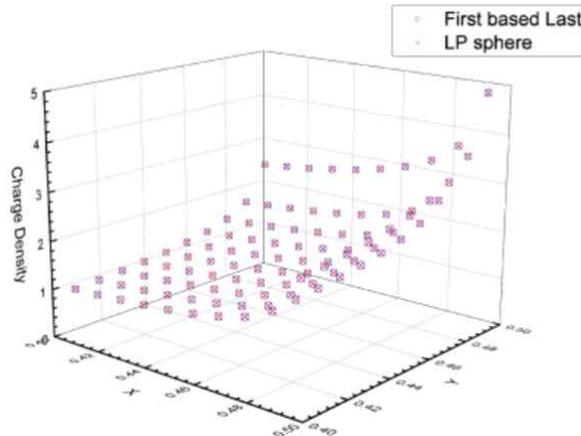
Jinseong Son<sup>1</sup>, Maximiliano Islas Solis<sup>2</sup>, Tsoggerel Tsogbadrakh<sup>2</sup> and Chi-Ok Hwang<sup>2\*</sup>

<sup>1</sup> No Affiliation, Republic of Korea

<sup>2</sup> Gwangju Institute of Science and Technology, Gwangju 61005, Republic of Korea

Corresponding author (Electronic mail: [chwang@gist.ac.kr](mailto:chwang@gist.ac.kr))

According to probabilistic potential theory, first- and last-passage algorithms have been developed. Usually the first-passage algorithms with an enclosing sphere are used for overall charge distribution on a closed conducting object and last-passage algorithms for charge density at a specific point on the conducting object. The first- and last-passage algorithms are inherently connected. In this paper, we combine the first- and last-passage algorithms. We develop an algorithm for computing charge density at a specific point on the conducting object via the overall charge density distribution on a conducting object which is the simulation result of the first-passage algorithm with an enclosing sphere. We demonstrate the algorithm for charge density on a sphere and on the unit cube held at unit potential. The results show good agreements with theoretical or other simulation ones.



**Figure 1** The charge density of the upper surface of conducting unit cube obtained by first-passage-based last-passage algorithm and last-passage algorithm. The coordinate of the vertex of the cube is (0.5, 0.5). Charge density is Normalized by result of (0.405, 0.405).

**Acknowledgments** This work was supported by the GIST Research Institute (GRI) in 2024.

## References

- [1] J. Son, J. Im, and C.-O. Hwang, Appl. Math. Comput. submitted (2021).
- [2] H. Jang, U. Yu, Y. Chung, and C.-O. Hwang, Adv. Theory Simul. 3(8) (2020).
- [3] H. Jang, J. Given, U. Yu, and C.-O. Hwang, Adv. Theory Simul. <https://onlinelibrary.wiley.com/doi/full/10.1002/adts.202000268> (2021).
- [4] C.-O. Hwang and T. Won, J. Korean Phys. Soc. 47, S464 (2005).
- [5] J. A. Given, C.-O. Hwang, and M. Mascagni, Phys. Rev. E 66, 056704 (2002).